DEPARTMENT OF ENVIRONMENTAL PROTECTION

Commonwealth of Pennsylvania
State Board for Certification of Water and Wastewater Systems Operators
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## Formulas, Conversions, and Common Scientific Units



## Formulas,

Conversions
\& Abbreviations


Units of Weight, Volume, Time, Density, Concentration \& Flow

## Formulas \& Conversions

## Formulas

## AREA

Area of Rectangle $=($ Length $) \times($ Width $)$
Area of Triangle $=1 / 2 \times$ (Base) $\times$ (Height)
Area of Circle $=(0.785) \times\left(\right.$ Diameter $\left.^{2}\right)$ or (3.14) $\times\left(\right.$ Radius $\left.^{2}\right)$
Area of Cylinder Surface $=\left[(0.785) \times\left(\right.\right.$ Diameter $\left.\left.^{2}\right)\right]+[(3.14) \times($ Diameter $) \times($ Height $)]$
Circumference of Circle $=(3.14) \times$ (Diameter) or (2) $\times$ (3.14) $\times$ (Radius)
Curved Surface Area of a Cylinder $=(2) \times(3.14) \times$ (Radius) $\times$ (Height)
End Surface Areas of a Cylinder (both ends) = (2) x (3.14) x $\left(\right.$ Radius $\left.^{2}\right)$

## VOLUME

Volume of Rectangular Tank $\left(\mathrm{ft}^{3}\right)=($ Length $) \mathrm{x}($ Width $) \times($ Height $)$
Volume of Cone $\left(\mathrm{ft}^{3}\right)=(.333) \times(0.785) \times\left(\right.$ Diameter $\left.^{2}\right) \times($ Height $)$
Volume of Cylinder $\left(\mathrm{ft}^{3}\right)=(0.785) \times\left(\right.$ Diameter $\left.{ }^{2}\right) \mathrm{x}($ Height $)$ or (3.14) $\times\left(\right.$ Radius $\left.^{2}\right) \times($ Height $)$
Volume of a Treatment Vessel, gal $=$ Volume $\left(\mathrm{ft}^{3}\right) \times\left(7.48 \mathrm{gal} / \mathrm{ft}^{3}\right)$

## WATER FORMULAS

Alkalinity $=(\mathrm{mL}$ of Titrant) (Acid Normality) $(50,000)$ mL of Sample

Chlorine Demand (mg/L) = Chlorine dose - chlorine residual
$\mathrm{CT}=$ Concentration of disinfectant residual X contact time (mins)
Detention Time (minutes) = Volume of Tank (gallons) Influent Flow (gpm)

Dilution Formula:
Volume of Solution 1 (gal) x \% of Solution 1 = Volume of Solution 2 (gal) x \% of Solution 2
Discharge $=$ Volume
Time
Dose, $\mathrm{mg} / \mathrm{L}=$ Feed Rate, lbs/day
(Flow, MGD) x ( $8.34 \mathrm{lbs} / \mathrm{gal}$ )

Dry Chemical, lbs. $=8.34 \times$ Volume (gallons) $\mathrm{x} \%$ Solution (as a decimal)

$$
\text { Efficiency, } \%=\frac{\text { In }- \text { Out }}{\text { In }} \times 100
$$

Feed Rate, lbs/day = (Flow, MGD) x (Dosage, mg/L) x (8.34 lbs/gal)
Feed Rate, gal/day = (Flow, MGD) x (Dosage, mg/L) x (8.34 lbs/gal)
(Active ingredient weight (lbs/gal)

Filter Backwash or Loading rate $=$ Flow (gpm)
Filter surface area ( $\mathrm{ft}^{2}$ )

Hardness $=(\underline{m L}$ of Titrant) $(1,000)$ (for 0.2 N EDTA) mL of Sample

Horsepower (hp):
Motor hp $=($ Flow, gpm) $($ Total Water Head, ft $)$ 3960

Brake hp = Motor hp pump efficiency

Ion Exchange Regeneration Brine (gal) = Salt dosage (lbs/ft3) x Volume of Resin (ft3) Brine solution active strength (lbs/gal)

Reduction in Flow, \% = (Original Flow - Reduced Flow) (100\%)
Original Flow
Surface Loading Rate $\left(\mathrm{gpd} / \mathrm{ft}^{2}\right)=$ Flow Rate, gpd Surface Area, $\mathrm{ft}^{2}$

UV Absorbance (A) = Log (100\%/\%T) where T = I/I.
I = Intensity at sensor (milliwatts per square centimeter)
$\mathrm{I}_{0}=$ Intensity at source (milliwatts per square centimeter)
$\mathrm{T}=$ Transmittance
Velocity = Flow or Distance
Area Time
Weight of a liquid, lbs = gallons x Specific Gravity x $8.34 \mathrm{lbs} / \mathrm{gal}$
Weight of active ingredient, lbs = gallons x Specific Gravity x $8.34 \times \%$ solution (as a decimal)

## WASTEWATER FORMULAS

Chlorine Demand (lbs/day) = Dose (lbs/day) - Residual (lbs/day)
Detention Time $=\frac{\text { Volume of Tank }}{\text { Influent Flow }}$
Efficiency, \% removal $=\frac{\text { In - Out }}{\text { In }} \times 100$
Food/Microorganism Ratio $=$ Influent BOD, lbs/day MLVSS, lbs

Horsepower (hp):

$$
\text { Motor } \mathrm{hp}=\frac{(\text { Flow, } \mathrm{gpm}) \mathrm{x}(\text { Total Water Head, ft })}{3960}
$$

Brake hp $=\underset{\text { pump efficiency }}{\text { Motor } \mathrm{hp}}$
Hydraulic Surface Loading Rate (gpd/ft ${ }^{2}$ ) = Flow Rate (gpd) Surface Area ( $\mathrm{ft}^{2}$ )

Load, lbs $=($ Concentration, mg/L) $\times($ Volume, mil. Gal $) \times 8.34$
Loading, lbs/day = (Concentration, mg/L) x (Flow, MGD) x 8.34
Mean Cell Residence Time (MCRT) =
(Suspended Solids in Aeration System, lbs)
( Suspended Solids Wasted, lbs/day + Suspended Solids Lost in Effluent, lbs/day)
Organic Loading Rate Trickling Filter $=$ Organic Load $(B O D), \mathrm{lbs} /$ day $\times 1,000 \mathrm{ft}^{3}$
Volume, $\mathrm{ft}^{3}$
Oxygen Uptake = Oxygen Usage (mg/L) Time (min)

Pump rate $=$ Volume
Time
Slope $=$ Drop or Rise
Distance
Sludge Volume Index $=(\underline{\text { Settleable Solids, } \%) \times(10,000)}$
MLSS, mg/L

Solids Loading Trickling Filter, (lbs/day/ft ${ }^{2}$ ) = Solids Applied, lbs/day
Surface Area, $\mathrm{ft}^{2}$

Solids, mg/L = (Dry Solids, grams) $\mathrm{x}(1,000,000)$

> ML of Sample

Surface Loading Rate $\left(\mathrm{gpd} / \mathrm{ft}^{2}\right)=$ Flow Rate, gpd Surface Area, $\mathrm{ft}^{2}$

Velocity = Flow or Distance Area Time

Volatile Solids, \% = (Dry Solids - Ash Solids) x (100\%) Dry Solids

Weir Overflow Rate $=$ Flow (gpd)
Weir Length, (ft)
Weight of a liquid, $\mathrm{lbs}=$ gallons x Specific Gravity x 8.34

## Conversion Factors:

| 1 acre $=43,560$ square feet | 1 horsepower $=0.746$ kilowatts |
| :--- | :--- |
| 1 cubic foot $=7.48$ Gallons | 1 million gallons per day $=694$ gallons per minute |
| 1 foot $=0.305$ meters | 1 pound = 0.454 kilograms |
| 1 gallon $=3.79$ liters | 1 pound per square inch $=2.31$ feet of water |
| 1 gallon $=8.34$ pounds | Degrees Celsius $=($ Degrees Fahrenheit -32$)(5 / 9)$ |
| 1 grain per gallon $=17.1 \mathrm{mg} / \mathrm{L}$ | Degrees Farenheit $=($ Degrees Celsius x 1.8$)+32$ |
| $1 \mathrm{mg} / \mathrm{L}=1 \mathrm{ppm}$ | 1 Ft of water column = 0.43 psi |

Abbreviations:

| BOD | Biochemical Oxygen Demand |
| :--- | :--- |
| ft | feet |
| gpd | gallons per day |
| gpg | grains per gallon |
| gpm | gallons per minute |
| lbs | pounds |
| mg/L | milligrams per Liter |
| MGD | million gallons per day |
| mL | milliliter |
| MLSS | mixed liquor suspended solids |
| MLVSS | mixed liquor volatile suspended solids |
| ppm | parts per million |

## UNITS OF WEIGHT

| English | Metric |
| :---: | :---: |
| pound -lb | gram -g <br> milligram -mg <br> kilogram -kg |
| CONVERSIONS |  |
| Metric/Metric | Metric/English |
| $1000 \mathrm{mg}=1 \mathrm{~g}$ or $1000 \mathrm{mg} / \mathrm{g}$ |  |
| $1000 \mathrm{gm}=1 \mathrm{~kg}$ or $1000 \mathrm{~g} / \mathrm{kg}$ |  |$\quad$| $1 \mathrm{lb}=454 \mathrm{~g}$ or $454 \mathrm{~g} / \mathrm{lb}$ |
| :---: |


| UNITS OF VOLUME |  |  |
| :---: | :---: | :---: |
| English |  | Metric |
| ```gallon - gal million gallon - Mga cubic feet - cu ft``` |  | $\begin{gathered} \text { liter - L } \\ \text { milliliter - mL } \end{gathered}$ |
| CONVERSIONS |  |  |
| Metric/Metric | Metric/English | English/English |
| $\begin{gathered} 1000 \mathrm{~mL}=1 \text { liter or } 1000 \\ \mathrm{~mL} / \mathrm{L} \end{gathered}$ | $\begin{gathered} 1 \mathrm{gal}=3.785 \mathrm{~L} \text { or } 3.785 \\ \mathrm{~L} / \mathrm{gal} \\ 1 \mathrm{gal}=3785 \mathrm{~mL} \text { or } 3785 \\ \mathrm{~mL} / \mathrm{gal} \end{gathered}$ | $7.48 \mathrm{gal}=1 \mathrm{cu} \mathrm{ft}$ or 7.48 gal/cu ft |

## UNITS OF TIME

| day - day | minute - min |
| :--- | :--- |
| hour - hr | second - sec |

## CONVERSIONS

1 day $=24 \mathrm{hr}$ or $24 \mathrm{hr} /$ day
$1 \mathrm{hr}=60 \mathrm{~min}$ or $60 \mathrm{~min} / \mathrm{hr}$
$1 \mathrm{~min}=60 \mathrm{sec}$ or $60 \mathrm{sec} / \mathrm{min}$
1 day $=1440 \mathrm{~min}$ or $1440 \mathrm{~min} /$ day

| UNITS OF DENSITY |  |  |
| :---: | :---: | :---: |
| English |  | Metric |
| $\mathrm{lbs} / \mathrm{gal}$ | $\mathrm{kg} / \mathrm{L}$ |  |
| $\mathrm{lbs} / \mathrm{cu} \mathrm{ft}$ |  | $\mathrm{g} / \mathrm{mL}$ |
|  |  |  |
| English | THE DENSITY OF WATER |  |
| $8.34 \mathrm{lbs} / \mathrm{gal}$ |  | Metric/Metric |
| $62.4 \mathrm{lbs} / \mathrm{cu} \mathrm{ft}$ |  | $1 \mathrm{~kg} / \mathrm{L}$ |

## UNITS OF CONCENTRATION

| English |  | Metric |
| :---: | :---: | :---: | :---: |
| $\mathrm{lbs} / \mathrm{gal}$ | $\mathrm{mg} / \mathrm{L}$ |  |
| CONVERSIONS |  |  |
| $1 \mathrm{lb} / \mathrm{gal}=120,000 \mathrm{mg} / \mathrm{L}$ |  |  |


| UNITS OF FLOW |  |
| :---: | :---: |
| English | Metric |
| ```gallons per minute - gal/min - GPM gallons per day - gal/day - GPD million gallons per day - Mgal/day - MGD cubic feet per second - cu ft/sec - CFS``` | milliliters per minute - mL/min |
| CONVERSIONS |  |
| English/English | English/Metric |
| 1 MGD $=694$ GPM or 694 GPM/MGD <br> 1 MGD $=1.55$ CFS or 1.55 CFS/MGD | $1 \mathrm{gal} /$ day $=2.63 \mathrm{~mL} / \mathrm{min}$ |

## Davidson Pie



